Reverse Engineering the NAEP Floating Pencil Task Using the PADI Design System

Kathleen C. Haynie, Kathleen Haynie Consulting
Geneva D. Haertel, SRI International
Andrea A. Lash, SRI International
Edys S. Quellmalz, SRI International
Angela Haydel DeBarger, SRI International
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Prepared by:
Kathleen C. Haynie, Kathleen Haynie Consulting
Geneva D. Haertel, SRI International
Andrea A. Lash, SRI International
Edys S. Quellmalz, SRI International
Angela Haydel DeBarger, SRI International
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Large-scale science assessments have been criticized for not tapping rich, authentic scientific problems. The use of evidence-centered design (ECD) principles in large-scale assessment design can potentially improve the quality of performance assessment tasks for scientific inquiry. The Principled Assessment Designs for Inquiry (PADI) design system has been used by the PADI team to analyze several well-known science assessments. This report will discuss the reverse engineering of the National Assessment of Educational Progress (NAEP) Floating Pencil task. The PADI design system was used as an analytical tool for understanding the characteristics and underlying assessment argument of this chosen task. Carrying out this work, we grappled with task complexity and came to understand how science performance assessment tasks might be constructed in the future.

In reverse engineering the Floating Pencil task into an assessment blueprint, our team created a task specification on the PADI design system. In designing the Floating Pencil task specification, we specified the Task Model, Student Model, and Evidence Model. In defining the Task Model, we considered what family of tasks Floating Pencil might be a member of—helping to define the fixed characteristics and Task Model Variables for Floating Pencil. Our team considered a variety of potential Student Models and chose one based on the NAEP content-by-process framework (Allen, Carlson, & Zelenak, 1999). The chosen Evidence Model included an evaluative submodel that mirrored NAEP’s rubric for Floating Pencil (publicly released, see <http://listserv.aaia1.k12.ia.us/science/96sci8.pdf>). We defined unidimensional Rasch Measurement Models for each Activity within Floating Pencil.

The use of the PADI design system to reverse engineer the Floating Pencil task resulted in the creation of new assessment knowledge, general and specific to Floating Pencil, for our team and the PADI project. We considered the coherence and linkages among the Task Model, Student Model, and Evidence Model and grappled with the underlying assessment argument for Floating Pencil. Reverse engineering the Floating Pencil task not only contributed to our knowledge of the characteristics of one particular large-scale performance assessment task, but shed light on how new science performance assessments might be forward engineered.
1.0 Introduction

Performance assessment tasks for scientific inquiry have been utilized in large-scale reference examinations, such as the National Assessment of Educational Progress (NAEP) and the Trends in International Mathematics and Science Study (TIMSS). Since large-scale assessment results can be used to provide policymakers and the public with information about how U.S. students perform in different content areas, the intelligent design of these performance assessment tasks is of paramount importance to the validity of large-scale examinations. The validity of science performance assessments has received mixed reviews (Bass, Magone, & Glaser, 2002; Shavelson & Ruiz-Primo, 1998; Shepard et al., 1995). Large-scale science assessments have been criticized for not tapping rich, authentic scientific problems.

The use of evidence-centered design (ECD) principles in large-scale assessment design can potentially improve the quality of performance assessment tasks for scientific inquiry. The Principled Assessment Designs for Inquiry (PADI) design system has been used by the PADI team to analyze several well-known science assessments. This work has led to understandings of the complexity of such tasks and of how such tasks might be constructed in the future.

This report will discuss the process by which the PADI design system was used as an analytical tool for understanding the characteristics of a chosen NAEP performance assessment task. It was expected that by systematically reverse engineering an inquiry task and its key elements, we would grapple with task complexity in such a way that new understandings of the design process for such tasks could emerge. This report will describe how a performance assessment task was selected and analyzed, via reverse engineering, through the lens of ECD principles. In addition, this report will discuss the construction of an underlying assessment argument for the performance assessment task.
2.0 The PADI Project

Principled Assessment Designs for Inquiry was funded in 2002 by the Interagency Education Research Initiative (IERI). PADI draws on new understandings in cognitive psychology, research on science inquiry, and recent advances in measurement theory and technology to create a conceptual framework and supporting web-based software that educators are able to use to design inquiry assessments. Designing systems for assessing inquiry in science requires expertise across domains: science content and learning, assessment design, task authoring, psychometrics, delivery technologies, and systems engineering. The goal of the PADI project is to provide a conceptual framework for designing inquiry tasks that coordinates such expertise and provides supporting tools to facilitate use. PADI seeks to provide a practical, theory-based approach to developing high-quality assessments of science inquiry (Mislevy, Chudowsky, et al., 2003) by developing multiple components: (1) a system for designing reusable assessment task templates, organized around schemas of inquiry from research in cognitive psychology and science education; (2) generally stated rubrics for recognizing and evaluating evidence of inquiry skills; (3) an organized set of assessment development resources; (4) an initial collection of design patterns and exemplar templates and task specifications that are either forward or backward engineered; and (5) scoring engine and reporting tools that support more complex assessments and their statistical models.

2.1 Evidence-Centered Design

PADI is a special-case implementation of the evidence-centered design (ECD) framework developed by Mislevy, Steinberg, and Almond (2002). The ECD framework is based on a construct-centered approach to assessment (e.g., Messick, 1994) and describes the three components of assessment design: a Student Model, an Evidence Model, and a Task Model (Mislevy, Steinberg, Almond, Haertel, & Penuel, 2003). These components, taken together, comprise the assessment argument for a given task or assessment. The assessment argument lays out the links between the constructs one wishes to measure (Student Model), what serves as evidence of those constructs (Evidence Model), and what prompts students to respond in ways that can serve as evidence (Task Model). The stronger the links are between evidence and claims of student competencies, the stronger the likelihood of a valid measure for assessing the specified constructs.

For a given assessment, the Student Model addresses the question of what complex or set of knowledge, skills, or other attributes should be assessed. Student Model Variables (SMVs) are the underlying constructs an assessment is designed to assess. These constructs may be based on any theory of learning or psychological perspective (e.g., behaviorism, cognitive psychology, constructivism, situated cognition).

The Evidence Model addresses the question of what student behaviors or performances are expected to reveal those constructs. The Evidence Model lays out the argument for why and how the observations from a given task constitute evidence of scores or values on SMVs. The Evidence Model includes the evaluative submodel and the statistical submodel. The evaluative submodel provides the rules for evaluating evidence (e.g., a circled letter A on a multiple-choice item is evaluated as correct), which result in Observable Variables (e.g., a score of 1 is

---

1 Components of the ECD framework and assessment objects of the PADI design system will be capitalized throughout this report.
given to a student’s Work Product evaluated as correct). The statistical submodel describes a mathematical function that relates the Observable Variable to the SMV(s) (e.g., a logistic function models the positive relationship between student ability on an underlying SMV and the probability of answering an item correctly). Poor “fit” of a model to the empirical data—when data do not constitute strong evidence for the SMVs—may lead to a change or “update” of the Student Model.

The Task Model addresses the question of what tasks or situations should elicit the desired behaviors or performances identified in the Evidence Model. A Task Model describes circumstances meant to elicit information about what an examinee knows or can do. A Task Model provides a framework for describing the situation in which examinees act; such environmental specifications can include instructions, tools, lab materials, and characteristics of stimulus material that are considered Materials and Presentation. The Task Model also includes specifications for the form of an examinee’s response (e.g., a written essay, data represented on a graph), called a Work Product.

### 2.2 The PADI Design System

A primary deliverable of the PADI project is the specification of a modeling framework for the assessment of scientific inquiry. The PADI project created a web-based tool, the PADI design system, for manipulating examples that use this framework. The design system employs the Example-based Modeling (EMo) system (Schank & Hamel, 2004). A secondary deliverable for PADI is a library of examples of assessment blueprints. The design system serves as a repository or library of examples and as an editing tool to create and adapt the library. Some of the more complete examples in the library may serve as blueprints from which science assessments can be developed.

The design system employs a divide-and-conquer strategy, separating various parts of an assessment into chunks, or assessment objects, such as design patterns, templates, Work Products, Student Models, and so on (Riconscente, Mislevy, Hamel, & PADI Research Group, 2005). Figure 1 provides an overview of the relationships among these chunks or assessment objects. Design patterns (the orange object in Figure 1) are abstractions of common assessment practices, providing a theoretical underpinning for design practices. Design patterns can be helpful in introducing users to the PADI design system; an empty design pattern invites users to specify an assessment argument, explicating the relationship between Student, Evidence, and Task Models in a narrative form. In contrast, a template (the large object outlined in blue in Figure 1) is a second-layer abstraction that contains more specific information about the interrelations of Student, Evidence, and Task Models. Templates include the “nuts and bolts” details of the Activities, Measurement Models, Evaluation Phases, Work Products, Materials and Presentation, and Task Model Variables. Templates can be relatively abstract, such as when they represent a large family of tasks, and they can exist in hierarchies of specificity. When a template is very specific and complete, it is called a task specification, the blueprint that an authoring system can use to create actual assessment tasks. Task specifications may contain only one specific Student Model and must have fixed settings for all Task Model Variables and for Materials and Presentation choices.

2. The PADI project does not promise to provide the authoring and delivery procedures that result from using a task specification blueprint. Rather, the authoring and delivery systems are external to the PADI design system.
The PADI design system acts as a repository for a collection of design patterns, templates, and task specifications based on some real-world applications, including those of BioKIDS (<http://www.biokids.umich.edu/>), GLOBE (<http://www.globe.gov/fsl/educorn/assessment/assessments.html>), and FOSS (<http://lhsfoss.org/scope/research/projects.html>). Although only task specifications serve as genuine blueprints for authoring assessments, all three layers of representations (design patterns, templates, and task specifications) can be used en route to generating new assessment tasks.

The PADI design system provides tools for users. These include diagrams of interrelationships among PADI objects (such as Figure 1), definitions of PADI objects via a glossary and embedded help buttons, and links to PADI technical reports.

PADI project staff function as a networked, collaborative work team, in interaction with the PADI design system. For the PADI team, collaborative activities have contributed to the development of the PADI design system itself, design patterns, templates, and task specifications, a data management tool, and wizards (which facilitate the user interface with the

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3 Forthcoming technical reports will describe the applications of these science projects in the PADI design system.
4 For example, as part of the work of the GLOBE strand, a design pattern called “Conduct Investigations” was developed from one of the National Science Education Standards (NSES) inquiry standards (National Research Council, 1996) and is included in the repository. A second example in the repository is the template “ASK Performance,” part of the FOSS application, which gives specifications for a family of performance tasks assessing inquiry; the template presents three possible Student Models—unidimensional inquiry, multidimensional inquiry, and inquiry for diagnostics. One example of a task specification was reverse engineered from one of a set of existing tasks called “Mystery Boxes” (see Baxter, Elder, & Glaser, 1996); this task specification represents the first of six Mystery Box tasks, based on a one-variable Student Model that reflects a student’s understanding of how to construct a circuit and how to problem-solve with circuits.
The PADI Project

The PADI team is composed of expert psychometricians, cognitive scientists, software developers, science content specialists, assessment designers, evaluators, and engineers; thus, expertise is distributed. Members of the PADI project are networked across different sites and institutions: SRI International, University of Maryland, UC Berkeley, Lawrence Hall of Science, and University of Michigan. The PADI project has developed assessment designs for three K-12 science curricular programs, BioKIDS (Gotwals & Songer, 2006), FOSS (Timms & Kennedy, 2005), and GLOBE (DeBarger, Yumoto, & Quellmalz, 2005). In addition, there are several research and development strands that include template object modeling, scoring and calibration engine, design principles, the reverse engineering of several performance assessment tasks, and an implementation of the four-process delivery system. Taken as a whole, these strands contribute to the technical infrastructure and theoretical framework associated with the PADI design system and the knowledge base related to interactions between the PADI design system and assessment materials.

Because the PADI project focuses on a variety of types of scientific inquiry measures, a new PADI strand was created to examine inquiry measures from large-scale reference examinations. We understood that large-scale science assessments had a number of item sets or tasks that involved problem solving for some phase or phases of scientific inquiry. Our intention was to analyze and reverse engineer science inquiry tasks from large-scale reference examinations. Such work could lead to understandings of the complexity of such tasks and of how such tasks might be constructed in the future.

Our approach for this new strand of PADI work was collaborative—our team had seven members: a psychometrician, four educational psychologists, an assessment designer, and an engineer. One of PADI's Co-Principal Investigators, Geneva Haertel, was the leader of this project strand; the other Co-Principal Investigator, Robert Mislevy, frequently contributed to team meetings. Our team spanned two sites: SRI International in California and a site in New Jersey. Our team communicated via e-mail, periodic conference calls, and informal conversations. In addition, we joined the PADI project's weekly conference call meetings; these served a communicative and educational function for our team members. Our team worked in real time with the PADI design system—discussing conceptual ideas and assessment objects, entering new information, and revising our work.

This report will discuss the process by which this team accomplished its goal of using the PADI design system as an analytical tool for understanding the characteristics of a chosen inquiry task. In doing that, we will focus on one guiding question: In reverse engineering an existing inquiry task into a task specification, what did our team learn about the task's design features and properties and the task's underlying assessment argument?
3.0 Selection of a Performance Assessment Task

The initial goal of our team was to select an inquiry task to analyze and reverse engineer, using the PADI design system. Over the course of a year, the work of this PADI strand moved through two stages: (1) the selection of a particular inquiry task to reverse engineer and (2) the analysis and reverse engineering of the selected task, which resulted in the development of a task specification. This section describes how we selected a performance assessment task to reverse engineer. Following that, we will discuss what was learned in analyzing the task and carrying out the reverse engineering process that resulted in a task specification. These latter stages will be described through the lens of the ECD framework (i.e., how we developed the Student, Evidence, and Task Models).

3.1 What Is Reverse Engineering?

Reverse engineering is the process of creating a design or blueprint by analyzing a final product or system—often via identification of system components and their interrelationships—and creating representations of that product or system in an enhanced form or at a higher level of abstraction (e.g., see IEEE, 2003). In reverse engineering an existing task using the PADI design system, the task is parsed according to the attributes of the assessment objects that compose the Student, Evidence, and Task Models. Such parsing requires in-depth analysis of the task and typically results in a “trace” of the analysis work—a PADI representation in the form of a design pattern, template, or task specification. For example, using the template form requires defining an Activity (typically based on an item or group of items) that is composed of a specific Measurement Model, Evaluation Procedures, Work Product(s), Materials and Presentation, Presentation Logic, and Activity-level Task Model Variables (see Figure 1). The Measurement Model includes a definition of model type (e.g., dichotomous, partial credit), an Observable Variable, SMV(s), a Scoring Matrix, and a Design Matrix. The Evaluation Procedures include at least one Evaluation Phase in which Task Model Variables, Input Observable Variable(s) such as Work Products, Output Observable Variable(s), and Evaluation Action Data (e.g., the mapping of student Work Products onto Observable Variables) are specified.

3.2 Task Selection

For this PADI strand, the intention of the analysis work was to use the design system to understand the key characteristics of a selected inquiry task from a large-scale reference examination. Large-scale science assessments have been criticized for not tapping rich, authentic scientific problems. We expected that by systematically reverse engineering an authentic, multistep inquiry task and identifying its key elements (including the underlying assessment argument), we would grapple with task complexity in such a way that new understandings of the design process for such tasks could emerge.

Our pool of available items was drawn from large-scale reference examinations. A group of 46 such items from the NAEP, TIMSS, and New Standards science assessments were made available in June 2005 through the SRI study of middle school science, Validities of Standards-Based Science Inquiry Assessments: Implementation Study (see Quellmalz et al., 2004; Quellmalz & Haydel, 2003; and Quellmalz & Kreikemeier, 2002). These items were rated by a panel of science
education experts and received ratings for dimensions of inquiry from the National Science Education Standards.

We arrived at a basis for selecting a set of items or a task to reverse engineer. Our criteria for selecting a task or set of items included that it

- be part of the pool of released NAEP, TIMSS, and New Standards science items,
- contain items interconnected in some way as themes, blocks, or performance assessments, or based on some set of common qualities,
- involve multiple steps, and
- be considered a complex inquiry task, rather than a simple and easy task.

Items were required to be released (nonsecure) so that our analysis and reverse engineering work could be documented appropriately and shared with a wide audience. We expected that this task or set of items would be connected according to some theme, idea, or common stimulus, thus prompting examinee engagement with some aspect of inquiry. To best measure a phase or phases of the inquiry process, we expected that this task or set of items would be complex and require multiple steps. Of the available set of large-scale assessment items, we wanted to identify the richest possible measure of inquiry.

The available items were analyzed, in terms of their natural groupings or themes (e.g., links to a common stimulus or common topic), as measures of scientific inquiry. We looked at the distribution of tasks and item groupings across the NSES inquiry standards\(^5\) (National Research Council, 1996) to see which were more typical measures (e.g., of students' abilities to conduct an investigation) and which were less typical measures (e.g., of students' abilities to identify questions that can be investigated). For example, many of the available item groupings and tasks included items coded for NSES inquiry standard B, “Design and conduct a scientific investigation”; however, none of the available groups included items coded for NSES inquiry standard G, “Communicate scientific procedures and explanations.” We also considered the distribution of inquiry skills within tasks or item groupings, to see which groupings covered multiple skills and which measured only one skill. For example, Table 1 indicates that the Floating Pencil task, consisting of 14 items, covered 5 of the 8 NSES inquiry standards (see Quellmalz & Kreikemeier, 2002).

We selected a set of items—the NAEP Floating Pencil performance assessment for eighth grade—for analysis and reverse engineering (see Appendix A for a copy of the 14-item test booklet\(^6\)). Table 1 indicates that this task is associated with a range of NSES inquiry standards related to conducting a scientific investigation. All of the items within the task are linked to a common stimulus. In comparison with other available item groupings, this multistep performance assessment involves more phases of the inquiry cycle.

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\(^5\) The NSES inquiry standards refer to eight components of the grades 5–8 Content Standard A, “Abilities Necessary to Do Scientific Inquiry” (National Research Council, 1996, Chapter 6, pp. 145 & 148). For our convenience, we have labeled these eight components of scientific inquiry ability as inquiry standards A through H. Within each inquiry standard, we have denoted and labeled a number of substandards.

\(^6\) Note that there are 12-item and 14-item versions of the eighth-grade Floating Pencil task. The 14-item version was made available to SRI International as part of the Validities of Standards-Based Science Inquiry Assessments: Implementation Study (Quellmalz et al., 2004; Quellmalz & Hayden, 2003; Quellmalz & Kreikemeier, 2002); O’Sullivan, Reese, and Mazzeo (1997) provide a summary and description of this task. The 12-item version of the task (items 1-12 of the 14-item version provided in Appendix A) is publicly released and available, for example, at <http://nces.ed.gov/nationsreportcard/itmrls/sampleq/96sci8.pdf>.
Table 1. Distribution of NSES Inquiry Skills within the Floating Pencil Task

<table>
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<tr>
<th>NSES Standard / Substandard</th>
<th>Floating Pencil Item or Item Cluster</th>
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<tr>
<td></td>
<td>1</td>
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<tr>
<td><strong>B: Design and conduct a scientific investigation</strong></td>
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<tr>
<td>B1. Identify and control appropriate variables</td>
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<tr>
<td>B2. Collect systematic observation and/or detect inaccuracies</td>
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<tr>
<td>B3. Collect accurate measurements and/or detect errors</td>
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<tr>
<td>B4. Describe how to interpret/analyze data</td>
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<tr>
<td><strong>C: Use appropriate tools and techniques to gather, analyze, and interpret data</strong></td>
<td></td>
</tr>
<tr>
<td>C1. Use tools and techniques to gather data</td>
<td></td>
</tr>
<tr>
<td>C2. Use tools and techniques to organize data</td>
<td></td>
</tr>
<tr>
<td><strong>D: Develop descriptions, explanations, predictions, and models using evidence</strong></td>
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</tbody>
</table>
| D1. Describe observation: visually | | | | X | | | | | | X
| D1. Describe observation: mathematically | | | | X | | | | | | X |
| D1. Describe observation: comparison | | | | | | | | | X | |
| D2. Use evidence, subject matter knowledge, and argument to explain | | | | X | | | | X | |
| D3. Use evidence, subject matter knowledge, and argument to predict | | | | X | X | | | | |
| D4. Use evidence, logical argument, and subject matter knowledge to create models | | | | | | | | | | |
| **E: Think critically and logically to make the relationships between evidence and explanations** | | | | | | | | | | |
| E1. Decide what evidence to use | | | | | | | | | | |
| E2. Decide how to account for anomalous data | | | | | | | | X | | |
| E3. Review and summarize data to form logical argument | | | | | | | | | | |
| E4. Describe/explain possible cause-effect relationship | | | | | | | | X | | |
| **H: Use mathematics in all aspects of scientific inquiry** | | | | | | | | | | |
| H1. Use math to structure explanations | | | | | | | | | X | |
| H2. Use math to gather, organize, and present data | | | | | | | | X | | |
| H3. Use math to answer questions: average | | | | | | | | X | | |
| H3. Use math to answer questions: length | | | | | | | | X | | |
| H3. Use math to answer questions: graph | | | | | | | | X | X |
3.3 Description of the Floating Pencil Task

For the Floating Pencil performance assessment task, each student is given a test booklet (see Appendix A), his or her own kit of standardized and safe laboratory materials, and time limits to complete the task. Standardized laboratory materials include three solutions with varying salt concentrations, a graduated cylinder, a pencil, and a ruler. The task prompts students to individually conduct a hands-on investigation in which the experimental procedure has been specified. Students are asked to carry out a procedure that includes taking two measurements of the length of a pencil floating above the surface of different liquids (water, a 25% salt solution, and an unknown solution) contained within a graduated cylinder, averaging the two measurements, graphing the results, and estimating the salt concentration of the unknown solution. Students are asked to explain why the pencil floats in water, why it is better to take two measurements, why the pencil floats at a different level in the salt solution, and how they determined the salt concentration of the unknown solution. Students also are asked to predict what would happen if they added more salt to the salt solution.
4.0 Analysis and Reverse Engineering of Floating Pencil

For the Floating Pencil team, our reverse engineering activity is the instantiation of the Floating Pencil task into the ECD framework using the tools and representational forms of the PADI design system. The major components of an assessment within the PADI design system are identified in Figure 1. Some of these components, such as Materials and Presentation or Work Products, are readily apparent and therefore might represent surface-level characteristics of the Floating Pencil task. For example, the Floating Pencil test booklet lists the laboratory materials (Appendix A, page 39); also, we can easily determine the forms of students’ responses or Work Products (e.g., circled letters for multiple-choice items, numerical responses, written explanations). Other assessment components are more abstract and require considerable thought and discussion for their construction. For example, the set of psychological constructs underlying the Floating Pencil task, called the Student Model, cannot be easily determined from reading the test booklet. Also, the relationships among Work Products, Observable Variables, and SMVs are not readily apparent; much discussion must be given to the choice of the Evaluation Procedures as well as the characteristics of the Measurement Model. Such assessment objects might represent deep-level characteristics of the Floating Pencil task.

Finally, it should be noted that some assessment objects (e.g., Task Model Variables) might represent both surface-level characteristics (e.g., the number and types of solutions) and deep-level characteristics (e.g., cognitive complexity).

The reverse engineering and analysis of Floating Pencil generally moved from surface-level to deep-level task characteristics. We initially identified aspects of the Task Model, such as Materials and Presentation and Work Products, and then analyzed aspects of the Student Model (e.g., SMVs) and of the Evidence Model (e.g., Evaluation Phases and the Measurement Model). Other PADI strands have conducted their reverse engineering work similarly—identifying surface characteristics of the task before constructing more abstract assessment components such as Student Models and Measurement Models.

Our team carried out some preliminary analyses of the Floating Pencil task using the design pattern and template forms in the PADI design system. After some initial exploration of assessment arguments and variable and characteristic features (via the design pattern) and of Student Models and SMVs (via the template), we decided to model the Floating Pencil task as specifically as possible by using a task specification. This meant that we intended to eventually arrive at a specific Student Model, Evaluation Model, Measurement Model, and set of Task Model Variables (with settings). In what follows, we will explicate our reverse engineering and analysis work for Floating Pencil that led to the NAEP Floating Pencil task specification. We will present a logical progression—first discussing the Task Model, followed by the Student Model, and finally the Evidence Model.

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Cognitive complexity, for the purpose of this analysis, is defined for a given item by (1) the number of pieces of information needed to reach a solution and (2) the types of processes or data transformations needed to reach a solution.

Using Figure 1, objects of the Task Model are colored green, Student Model Variables are colored purple, and components of the Evidence Model are colored yellow.

It should be noted that a priori specifications of Student Models can be considered ‘hypotheses’ for testing model fit via empirical analyses; this, as the reader will learn, is the case with Floating Pencil.
4.1 The Task Model

According to the principles of evidence-centered design (Mislevy, Steinberg, & Almond, 2002), a Task Model provides a framework for describing the situation in which examinees act. Such environmental specifications can include instructions, tools, lab materials, characteristics of stimulus material that are considered Materials and Presentation, and other characteristics of the task itself. Task Model Variables represent some surface-level and deep-level characteristics of the task and of the items or Activities that comprise the task. In defining the Task Model for Floating Pencil, our team considered Materials and Presentation, Work Products, the structure of items and Activities, and Task Model Variables. The relationship among these assessment objects is shown in Figure 1.

4.1.1 Materials

Identifying the materials for Floating Pencil was a logical place to begin our analysis and reverse engineering work. Our initial list of materials can be found in the Floating Pencil test booklet (see Appendix A, page 39)—a graduated cylinder, a short pencil with a thumbtack in the eraser, a bottle of water, a bottle of salt solution, a bottle of unknown solution, a metric ruler, and paper towels. Of course, materials also included the Floating Pencil test booklet. Our team coded information about materials into two areas of the task specification: (1) under Materials and Presentation Requirements on the summary page (see Appendix B for the summary page of the task specification), we noted that students were to receive a kit of laboratory materials and a test booklet, and (2) under template-level Materials and Presentation on the summary page (Appendix B), we created a new object for each of the laboratory materials. In creating the new objects, we created a new MIME type, called Laboratory Materials on the PADI system; one new Materials and Presentation object was created for each of the laboratory materials, of type Laboratory Materials. We later added more specific information about the various laboratory materials under Materials and Presentation Settings; for example, instead of just listing “a bottle of salt solution,” we included the setting “65 ml. of 25% salt solution in a 100 ml. plastic bottle at room temperature.”

The Floating Pencil team discussed how variations in the laboratory materials could impact the nature of the task itself. At the most elementary level, a different set of laboratory materials could change the nature of the task, and variations in a set of laboratory materials could change the difficulty of the task. For example, the fourth-grade version of Floating Pencil has materials similar to those of the eighth-grade version, but includes a printed ruler on the test booklet rather than the physical ruler provided with the eighth-grade version. The fourth-grade task also includes a red marker that is not included in the eighth-grade task. The printed ruler eliminates some confusion in taking measurements (e.g., mistakenly holding the ruler upside-down or backwards); students are instructed to use the red marker to note the water level before the pencil is added (and are subsequently asked about changes in the water level). In both cases, the materials used for the fourth-grade version are intended to make the task less difficult. Even slight variations in laboratory materials could impact task difficulty. For instance, if one group of students received a ruler with only centimeter markings and another group of students received a ruler with centimeter and inch markings, the second group of students might have more difficulty measuring pencil length in centimeters (the markings in inches would serve as a distractor to proper measurement). Based on these considerations, our team concluded it was absolutely necessary to standardize task materials and to specify those details.
of standardization (e.g., the amount of salt solution, the length and scales of the ruler) in the task specification.

4.1.2 Presentation

Elements of presentation for Floating Pencil include environmental specifications, administrative directions, and the task directive or problem-situation description. Environmental specifications include giving students enough space and light to lay out the equipment and perform the task, giving students the test booklet and laboratory materials, and assuring that all materials are standardized according to NAEP’s specifications. Administrative directions might include communicating the task time limit to the students, mentioning that students are required to read through and follow the instructions in the test booklet, and asking students to write their answers directly in the test booklet. In the test booklet (see Appendix A, page 39), students are given the written direction of checking to see that they have a complete set of laboratory materials. The task directive or problem-situation description is given on the next page of the test booklet. This directive includes a warrant for the Floating Pencil task (that every body of water has some concentration of salt), a description of the task activities (e.g., observing and measuring how much of the length of a pencil floats above liquids with different salt concentrations, estimating the salt concentration of an unknown solution), and further administrative instructions to the students (e.g., writing their response in the space provided in the test booklet). As with materials, our team coded information about presentation into two areas of the task specification: (1) under Materials and Presentation Requirements on the summary page (Appendix B), we summarized information about the environmental specifications and administrative directions, and (2) under template-level Materials and Presentation, we used the Problem Situation Description object (which was created by the GLOBE project) and created and used the Time Limit object.

Variations in the task presentation can impact the difficulty of the task itself. For example, if students are in an environment with inadequate lighting or space, they might not be able to give their best performances. Variations in the time limit could impact the speededness of the task—the extent to which students’ ability to work quickly is a factor on their test performance. Our team discussed that the provision of some of the task content knowledge in the directive—that concentrations of salt vary among different bodies of water—makes the task easier by scaffolding\textsuperscript{10} that content.

4.1.3 Work Products

Our team identified and considered the Work Products for Floating Pencil. Part of our process of identifying Work Products included performing the task itself (as examinees) and generating our own Work Products. Our initial understandings of Floating Pencil Work Products are examinees’ item responses as recorded in the test booklets. For example, item 1 prompts examinees to explain why the pencil floats in the water; an examinee’s written explanation is the Work Product. The Work Products for Floating Pencil are presented in Table 2. These include multiple-choice responses, explanations, numerical responses, and plotted points and lines drawn on graphs. Our team coded information about Work Products into two areas of the task specification: (1) under Work Product Summary on the summary page (Appendix B), we

\textsuperscript{10}Scaffolding is providing examinees with tools, information, or instructions such that a task or Activity previously unreachable by an average examinee becomes reachable.
summarized the Work Products for Floating Pencil, and (2) within each Activity, we created a link to a specific Work Product object. In doing this, we identified and added to the PADI design system three new Work Products: Numerical Response, Table Entry–Numerical Response, and Graphical Elements.

Table 2. Work Products for Floating Pencil

<table>
<thead>
<tr>
<th>Work Product (Type)</th>
<th>Item Type</th>
<th>Item Number(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Explanation</td>
<td>Essay</td>
<td>1, 6, 9, 14b</td>
</tr>
<tr>
<td>Circed Letter</td>
<td>Multiple-Choice</td>
<td>7, 10, 13</td>
</tr>
<tr>
<td>Table Entry–Numerical Response</td>
<td>Free Response (numerical)</td>
<td>3, 4, 8, 11</td>
</tr>
<tr>
<td>Table Entry–Numerical Response (numerical measurement(s))</td>
<td>Free Response (numerical)</td>
<td>3, 4, 8, 11</td>
</tr>
<tr>
<td>Numerical Response (numerical average)</td>
<td>Free Response (numerical)</td>
<td>5, 8, 11</td>
</tr>
<tr>
<td>Numerical Response (numerical estimate)</td>
<td>Free Response (numerical)</td>
<td>14a</td>
</tr>
<tr>
<td>Graphical Elements (line)</td>
<td>Free Response (graphical)</td>
<td>2</td>
</tr>
<tr>
<td>Graphical Elements (plotted points and line)</td>
<td>Free Response (graphical)</td>
<td>12</td>
</tr>
</tbody>
</table>

Our understanding of Work Products for Floating Pencil was impacted by the NAEP 1996 Floating Pencil scoring rubric (publicly released; see <http://listserv.aa1.k12.ia.us/science/96sci8.pdf>). The scoring rubric provides an evaluative scheme for mapping Work Products onto Observable Variables. For example, students’ explanations for item 1 can be rated as 4 = Complete, 3 = Essential, 2 = Partial, or 1 = Unsatisfactory/Incorrect, depending on the quality of the response. The NAEP rubric provides evaluative schemes, resulting in Observable Variables, for most, but not all, of the Floating Pencil items; in addition, some evaluative schemes apply to groups of items. The drawn line resulting from item 2 is not evaluated. Items 3, 4, 8 (numerical measurements), and 11 (numerical measurements), which all result in numerical measurement entries in a table, are scored using one evaluative scheme, resulting in one Observable Variable. Items 5, 8 (numerical average), and 11 (numerical average) also are scored using one evaluative scheme, resulting in one Observable Variable. Table 3 provides evaluative information for all 14 of the Floating Pencil items. To be consistent with NAEP, the Floating Pencil team decided to adopt the NAEP scoring rubric as the set of evaluative schemes for the Floating Pencil items.
Table 3. Scoring Rubric Information for Floating Pencil Items and Item Groups

<table>
<thead>
<tr>
<th>Item or Item Group</th>
<th>Activity</th>
<th>Response Type</th>
<th>Evaluative Scheme</th>
<th>Score Level (Observable Variable)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Item 1</td>
<td>Activity 1</td>
<td>Explanation</td>
<td>Quality of explanation is evaluated.</td>
<td>4 = Complete 3 = Essential 2 = Partial 1 = Unsatisfactory/Incorrect</td>
</tr>
<tr>
<td>Item 2</td>
<td>Not Applicable</td>
<td>Drawn Line</td>
<td>Not evaluated.</td>
<td>None</td>
</tr>
<tr>
<td>Items 3, 4, 8, and 11</td>
<td>Activity 2</td>
<td>Numerical Measurement (Table Entry)</td>
<td>Difference of repeated measurements and order of measurements by liquid type are evaluated according to tolerances.</td>
<td>4 = Complete 3 = Essential 2 = Partial 1 = Unsatisfactory/Incorrect</td>
</tr>
<tr>
<td>Items 5, 8, and 11</td>
<td>Activity 3</td>
<td>Numerical Average (Table Entry)</td>
<td>Averages are compared with original measurements and evaluated according to tolerances.</td>
<td>3 = Complete 2a = Partial 2b = Partial 1 = Unsatisfactory/Incorrect</td>
</tr>
<tr>
<td>Item 6</td>
<td>Activity 4</td>
<td>Explanation</td>
<td>Quality of explanation is evaluated.</td>
<td>3 = Complete 2a = Partial 2b = Partial 2c = Partial 1 = Unsatisfactory/Incorrect</td>
</tr>
<tr>
<td>Item 7</td>
<td>Activity 5</td>
<td>Circed Letter</td>
<td>Evaluated according to answer key.</td>
<td>1 = Correct 0 = Incorrect</td>
</tr>
<tr>
<td>Item 9</td>
<td>Activity 6</td>
<td>Explanation</td>
<td>Quality of explanation is evaluated.</td>
<td>3 = Complete 2 = Partial 1 = Unsatisfactory/Incorrect</td>
</tr>
<tr>
<td>Item 10</td>
<td>Activity 7</td>
<td>Circed Letter</td>
<td>Evaluated according to answer key.</td>
<td>1 = Correct 0 = Incorrect</td>
</tr>
<tr>
<td>Item 12</td>
<td>Activity 8</td>
<td>Plotted Points and Connecting Line</td>
<td>Plotted data points compared with original data and presence of a straight line are evaluated.</td>
<td>3 = Complete 2a = Partial 2b = Partial 1 = Unsatisfactory/Incorrect</td>
</tr>
<tr>
<td>Item 13</td>
<td>Activity 9</td>
<td>Circed Letter</td>
<td>Evaluated according to answer key.</td>
<td>1 = Correct 0 = Incorrect</td>
</tr>
<tr>
<td>Item 14</td>
<td>Activity 10</td>
<td>Numerical Estimate and Explanation</td>
<td>Consistency of numerical estimate with the data and quality of explanation are evaluated.</td>
<td>4 = Complete 3 = Essential 2 = Partial 1 = Unsatisfactory/Incorrect</td>
</tr>
</tbody>
</table>
4.1.4 Item and Activity Structure

Another aspect of constructing the Task Model involved defining Activities for Floating Pencil. As the reader may note in Figure 1, Activities constitute the major components of a template or task specification and are used to structure the generation, collection, and scoring of evidence. An Activity contains a group of related objects, including Materials and Presentation, Work Products, Evaluative Phases, Observable Variables, and Measurement Models. Activities can belong to multiple templates or task specifications, and a template or task specification can have one or more Activities. A task may have several distinct stages of investigation, and such stages act as a natural partitioning of the task into Activities. As we illustrated in the previous section, the Floating Pencil task consists of 14 items, some of which are scored together based on the NAEP scoring rubric. For the purposes of drafting our task specification, we considered any scored item or group of items scored together as one Activity because the result is a single Observable Variable. For Floating Pencil, we defined 10 Activities on the basis of the 14 items (see Table 3, first and second columns).

A critical aspect of structuring the task specification on the PADI design system was defining the relationship between the Floating Pencil Activities and the task itself. Our team discussed whether to create one task specification with 10 Activities or 10 separate task specifications, each with one Activity. Floating Pencil Activities are all dependent on a common task directive and on a set of physical stimulus materials. In addition, some Floating Pencil Activities are sequentially dependent—that is, the Work Product from one Activity serves as stimulus material for a subsequent item. Given these properties, we decided to reverse engineer the Floating Pencil task into one task specification with 10 Activities.

Our team created 10 Activities in the task specification. Information about Activities is represented in two areas of the task specification. Under Activities Summary on the summary page (Appendix B), we noted that the 1996 NAEP scoring rubric was used as the basis for our definition of an Activity and that the Floating Pencil task has a total of 10 Activities. We then defined the 10 Activities in the Activities section of the task specification summary page. Multiple objects were specified for each Activity; these components include Title, Summary, Measurement Models, Evaluation Procedures, Work Products, Materials and Presentation, Presentation Logic, and Task Model Variables. Our team defined Measurement Models and Evaluation Procedures for all Activities. Task Model Variables will be considered in the next section of this report. We also defined Work Products, Materials and Presentation, and Presentation Logic. For Activity 1 (see Figure 2), the Work Product was defined as Open-Ended Response. The materials included the test booklet, water, a graduated cylinder, and a pencil with a thumbtack in the eraser (these are a subset of the materials defined at the task specification level). The Presentation Logic notes the materials and conditions needed to begin the task, the Activity-level directions given to the student, and the expectation of a written student response.

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11 The decisions about whether to have several Activities and how to define the scope of an Activity are left to the assessment developer.

12 These will be discussed in subsequent sections of this report.
4.1.5 Task Model Variables

Central to a fully defined Task Model are Task Model Variables (TMVs). TMVs are conditions in the assessment task and its environment that can vary and thereby affect the assessment in a significant way. A TMV can represent a decision that an assessment designer makes before finalizing an assessment task, like the difficulty level of an item, or a condition in the administration of the task, like a time limit. TMVs can be surface-level characteristics, like the presence or absence of laboratory materials, or deeper-level (e.g., more abstract) characteristics, such as the cognitive complexity of an Activity. We have already suggested some potential TMVs in the context of Floating Pencil materials—for example, the amount of salt solution or the length and scales of the ruler. Our team also discussed how variations in the physical materials, such as the number of solutions, pencil thickness, and different water temperatures, might impact the Floating Pencil task. In terms of presentation, time limit is a TMV that can impact the speededness of the task. Also, the provision of content knowledge in the task directive may decrease the difficulty of Activities that require such content knowledge. The form of Work Products (e.g., a circled response measuring knowledge recognition versus an essay explanation measuring comprehension) is yet another TMV that can impact the difficulty of an Activity.

We sought to determine a workable set of TMVs for Floating Pencil. As we analyzed Floating Pencil and continued our reverse engineering work, we identified many TMVs. In fact, at one point we had a working list of over 40 TMVs, which included the number of distractors on a multiple-choice Activity, scaffolding levels for inquiry, the number of stimuli present for an Activity, the use of graphics for an Activity, and the width of horizontal and vertical units for a graphing Activity. It was clear that a nearly unlimited list of TMVs could be generated. Our team
then discussed the importance of narrowing our working list of TMVs to those that are important in describing key aspects of the task. Consider the analogy of a roadmap. A roadmap covering a wide distance probably would not indicate every potentially salient feature that exists (e.g., minor roads, every school); the map would be most useful if it included the important features needed to navigate over long distances (e.g., major highways, airports). Similarly, we needed to determine a comprehensive set of key TMVs for Floating Pencil. In doing this, members of our team noted that Floating Pencil was scaffolded procedurally and that the reading demands were high. We noted that for both content and inquiry we could consider the level of scaffolding, level of difficulty, and extensiveness. Our team discussed the research results (Bass, Magone, & Glaser, 2002; Baxter & Glaser, 1998) that identified the task as content-lean (low content extensiveness) and process-constrained (high scaffolding for inquiry).

In completing the task specification, we identified the following key TMVs: the physical materials of the task, the level of inquiry structure (including scaffolding, difficulty, and extensiveness of inquiry), the level of content structure (also including scaffolding, difficulty, and extensiveness), the verbal demand of the task, and the cognitive complexity of the task. In working with the task specification, our team came to understand that some TMVs can be specific to an Activity (e.g., the form of a Work Product) and others are pertinent to the task as a whole (e.g., scaffolding for inquiry). Our team coded information about TMVs into four areas of the task specification, the first three of which are found on the summary page (Appendix B): (1) under Task Model Variable Summary we noted the key TMVs listed above, (2) under template-level Task Model Variables we created links to the actual TMV objects representing the summarized categories, (3) under Task Model Variable Settings we provided the settings for each of the key TMVs at the task specification level (e.g., the level of inquiry scaffolding was set as high), and (4) within each Activity under Task Model Variables we linked to some key TMVs specific to each activity.

There was an ongoing interplay between our consideration of Task Model Variables and our conception of a family of tasks, of which Floating Pencil was a member. Our consideration of the research results for Floating Pencil (e.g., inquiry-constrained and content-lean) led us to consider other multistep performance assessment tasks with lower levels of scaffolding for inquiry. We began to think about what dimensions might vary across performance assessment tasks involving laboratory materials. At the core of understanding what can vary across a set of related tasks and conceptualizing a family of tasks (which could be defined through broader PADI representations like an abstract template) was this question: “What is the Floating Pencil task an instance of?” This question stimulated multiple conversations about a family of performance assessment tasks in which we discussed the basis for and characteristics of a task family. Toward this end, we analyzed a fourth-grade version of the Floating Pencil task. In comparison with the eighth-grade version of the task, the physical materials were similar, the directives differed, the number of activities differed, the number of skills assessed differed, and the cognitive complexity of the activities differed. As can be seen in Table 4, the content and inquiry skills assessed by the fourth- and eighth-grade versions of the task varied; for example, the fourth-grade version did not have any items rated for NSES inquiry standard B, “Design and conduct a scientific investigation.” We considered what a family of Floating Pencil tasks might look like, and that this family would be a subset of a general family of performance assessment tasks. We postulated some characteristics that might vary across a family of Floating Pencil
tasks: the numbers of activities, the numbers of skills assessed, the sequencing of cognitive complexity across the task, the presence or absence of graphing, the number of measurements taken, and the number of salt solutions. We also analyzed some available multistep performance assessment tasks involving laboratory materials.

Table 4. Comparison of Content and Inquiry Skills for Fourth- and Eighth-Grade Floating Pencil Tasks

<table>
<thead>
<tr>
<th>Content Knowledge</th>
<th>Grade 4</th>
<th>Grade 8</th>
</tr>
</thead>
<tbody>
<tr>
<td>Density/relative densities</td>
<td>Item 8, Item 10</td>
<td>Activity 1, Activity 2, Activity 5</td>
</tr>
<tr>
<td>Concentration of a solution</td>
<td>Item 8, Item 10</td>
<td>Activity 6, Activity 7, Activity 9, Activity 10</td>
</tr>
<tr>
<td>Constancy of volume</td>
<td>Item 2</td>
<td></td>
</tr>
<tr>
<td>Errors of measurement</td>
<td></td>
<td>Activity 4</td>
</tr>
<tr>
<td>Take and record measurement</td>
<td>Item 1, Cluster 4, 7, 9</td>
<td>Activity 2</td>
</tr>
<tr>
<td>Use ruler (physical) to measure length</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Use ruler (printed) to measure length</td>
<td>Cluster 4, 7, 9</td>
<td></td>
</tr>
<tr>
<td>Record data on cylinder</td>
<td>Item 2</td>
<td></td>
</tr>
<tr>
<td>Record data on diagram</td>
<td>Cluster 3, 6, 9, Cluster 4, 7, 9</td>
<td></td>
</tr>
<tr>
<td>Record data in table</td>
<td></td>
<td>Activity 2, Activity 3</td>
</tr>
<tr>
<td>Observe level of liquid</td>
<td>Item 1, Item 2</td>
<td></td>
</tr>
<tr>
<td>Observe pencil in liquid</td>
<td>Cluster 3, 6, 9, Item 5</td>
<td>Activity 1, Activity 2, Activity 5</td>
</tr>
<tr>
<td>Compare measurements</td>
<td>Item 10</td>
<td></td>
</tr>
<tr>
<td>How to plot values on XY graph</td>
<td></td>
<td>Activity 8</td>
</tr>
<tr>
<td>How to interpret graph</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**NSE Standard / Substandard**

**B: Design and conduct a scientific investigation**

| B2. Collect systematic observation and/or detect inaccuracies | Activity 4 |
| B3. Collect accurate measurements and/or detect errors       | Activity 4  |
| B4. Describe how to interpret/analyze data                   | Activity 1  |

**C: Use appropriate tools and techniques to gather, analyze, and interpret data**

| C1. Use tools and techniques to gather data                  | Cluster 3, 6, 9, Cluster 4, 7, 9 | Activity 2 |
| C2. Use tools and techniques to organize data               |                                       | Activity 8  |

**D: Develop descriptions, explanations, predictions, and models using evidence**

| D1. Describe observation: visually | Cluster 3, 6, 9, Cluster 4, 7, 9 | Activity 2, Activity 8 |
| D1. Describe observation: mathematically | Item 1, Cluster 4, 7, 9 | Activity 2, Activity 8 |
We postulated some characteristics of a family of science performance assessment tasks. These characteristics include tasks that:

- Involve standardized, externally supplied laboratory materials that are integral to the task, serving as stimulus materials among a set of activities.
- Provide a motivating question or problem to be investigated.
- Require students to work independently, implementing a solution strategy.
- Require the use of tools and techniques to gather data.
- Require the organization of data in a specified representational form.
- Elicit evidence for inquiry skills within particular science content domains.
- Could range in levels of verbal demand, difficulty, scaffolding, and cognitive complexity.

Our initial understandings of a potential family of tasks were based largely on the variation of Task Model Variables across similar and available science performance assessment tasks. These
understandings can begin to shed light on the question of how such tasks might be constructed in the future. However, to pursue this question in more depth, exploration is needed of the qualities of potential Student Models (underlying constructs to be measured) and Evidence Models (how evidence is evaluated and what the psychometric relationship is between observed evidence and underlying theoretical constructs).

4.2 The Student Model

Conceptually, a Student Model lays out the complex or set of knowledge, skills, or other attributes to be assessed by a task (Mislevy, Steinberg, & Almond, 2002). SMVs are the underlying constructs an assessment is designed to measure; also, SMVs are individual estimates of one facet of student proficiencies. An SMV is a part of at least one, and possibly more than one, Student Model. SMVs are the latent variables associated with a task—the knowledge, skills, or abilities the task is designed to elicit in the examinee. These latent variables can not be observed, and they typically refer to more abstract and theoretical constructs. An example of a Student Model is drawn from the Mystery Boxes task specification (Baxter, Elder, & Glaser, 1996). In this case, the task specification designers wished to measure students' abilities to construct a circuit and problem-solve with circuits. A Student Model was created, called “MB Circuitry Univariate,” that contained one SMV, called “MB SMV Univariate,” reflecting students' abilities to construct and problem-solve with circuits.

4.2.1 Exploration of Potential Student Models

A number of Student Models may be considered and used for a given task. For example, task specifications based on the Mystery Box task employ three different Student Models: MB Circuitry Univariate, MB Circuitry Multivariate, and MB Circuitry Multivariate with P-S. The SMV for MB Circuitry Univariate was described previously. The two SMVs for MB Circuitry Multivariate reflect students' abilities to identify a correct response from a list of choices and to provide evidence. MB Circuitry Multivariate with P-S has six SMVs, reflecting students' abilities to (1) select a correct answer, (2) provide evidence, (3) explain task-related concepts, (4) monitor their own progress, (5) plan for solving a task, and (6) strategically solve a task. Different Student Models may be developed for different purposes. The template ASK Performance, which gives specifications for a family of performance tasks assessing inquiry, presents three Student Models: ASK Unidimensional Inquiry, ASK MD Inquiry, and ASK MD Inquiry for Diagnostics. The unidimensional Student Model has one SMV—a variable of inquiry knowledge from which a single measure of inquiry could be derived (e.g., for reporting purposes). The multidimensional Student Model has four SMVs, based on different phases of the scientific inquiry process: design and conduct investigations, gather and organize data, interpret data, and construct an explanation using evidence. This Student Model was designed for use in charting student progress in using inquiry methods. Finally, the Inquiry for Diagnostics model also has four SMVs based on different phases of scientific inquiry; however, each SMV is divided into six or seven cutpoint-based categories. This Student Model is intended to produce measures useful for diagnosing student abilities.

Given an existing task to be reverse engineered, the Student Model can be determined though task analysis. This process involves analyzing the demands of the task in terms of cognitive

13 For more information on the ASK project, see <http://www.lawrencehallofscience.org/foss/newsletters/present/FOSS27.assessing.html>
factors that include types of knowledge required (e.g., particular science content knowledge) and reasoning processes required (e.g., explanations linking theory and evidence). This process is informed by any framework or information from the task developer, such as a content-by-process matrix. Analysis of task demands includes identification of particular skills required for task completion, such as using tools to collect accurate measurements. The core knowledge, understanding, and skills required for successful completion of a task form the Student Model. The components of the Student Model—specific knowledge, skills, and abilities—are defined as Student Model Variables. Consideration is given to the number and generality of the SMVs. These determine the grain size of the Student Model and are based on the assessment argument. For example, if the purpose of the task is to provide pass/fail decisions for individual science achievement at a national level, one or two SMVs (e.g., science content knowledge and inquiry ability) may be preferable to a larger set of SMVs.

Initially, our team explored the cognitive demands of each item group or Activity in Floating Pencil through a number of lenses. First, we took the assessment ourselves, noting the cognitive demands of each item. For example (see Appendix A), we noted that students would need to understand the concept of density to provide a correct explanation for item 1 (Activity 1) and know how to do linear interpolation to correctly respond to item 14 (Activity 10). Second, we used the NSES inquiry standards (National Research Council, 1996) and considered the specific content and inquiry demands of each Activity. We used the ratings of Floating Pencil item groups by expert scientists on the NSES inquiry standards (see Table 1), as well as our own team ratings of content coverage for the items. For example, item 9 (Activity 6) reads, “Why does the pencil float at a different level in the salt solution than in the water?” and was rated as inquiry standard D, substandard D2, “Use evidence, subject matter knowledge, and argument to explain”; the item was considered to require content knowledge of densities, relative densities, and concentrations of solutions. Last, we considered the framework used by NAEP, the developers of the Floating Pencil task. The NAEP framework is a 3 by 3 content-by-process matrix (Allen, Carlson, & Zelenak, 1999). The content categories are physical science, earth and space science, and life science; the process categories are conceptual understanding, practical reasoning, and investigation. Every NAEP science item is given one content code and one process code (see Table 5). For example, Activity 6 is coded for earth and space sciences and conceptual understanding within the NAEP framework.

| Table 5. NAEP Content and Process Codes for Floating Pencil Activities |
|-------------------|-----------------|-----------------|-----------------|
| **Content**       | **Scientific Investigation** | **Practical Reasoning** | **Conceptual Understanding** |
| Physical Sciences | Activities 2, 3, and 4       |                  |                  |
| Earth and Space Sciences | Activities 5, 8, and 10 | Activity 7      | Activities 1, 6, and 9 |
| Life Sciences     |                  |                  |                  |

Different ways of defining Student Models for Floating Pencil were considered. Potential Student Models had the following characteristics: (1) one SMV measuring science proficiency, (2) two SMVs measuring science content and inquiry, (3) a number of SMVs representing...
instructionally based variables (useful for formative classroom assessment purposes), (4) SMVs representing the NSES inquiry standards assessed by Floating Pencil, and (5) SMVs based on the NAEP content-by-process framework. Although the first potential Student Model had the appeal of providing a potentially powerful measure of scientific proficiency, this model would not produce information specific to the measurement of scientific inquiry. The second potential Student Model, measuring content and inquiry, offered no real advantage over collapsing the content and process codes based on NAEP’s framework since both yield a two-dimensional content-by-process Student Model. We briefly considered a Student Model that consisted of specific, instructionally linked SMVs. For example, item 7 reads, “Take the pencil and put it in the 25% salt solution in the cylinder, eraser-end down. How does the pencil float in this solution compared to how it floated in the water?” The possible responses are: “a. In the salt solution, more of the pencil is above the surface” and “b. In the salt solution, more of the pencil is below the surface.” An SMV that reflects the nature of students’ cognitive abilities required for item 7 (Activity 5) might be “The ability to interpret observations made during an investigation.” Measures of student abilities on such SMVs could be used to inform the teaching of science by making the underlying cognitive abilities clear. This approach to a Student Model was not pursued, however. Given that Floating Pencil is part of the NAEP assessment and was to be calibrated with a larger group of NAEP items,14 Student Models were needed that supported broad categories based on a widely accepted framework.

We also considered Student Models for Floating Pencil based on the NSES inquiry standards.15 This approach had a number of advantages. The NSES inquiry standards (National Research Council, 1996) are accepted as a benchmark for inquiry practices in the science education community. The pool of NAEP items available for calibrating along with the Floating Pencil task already had received expert ratings on the NSES inquiry standards. Also, the standards differentiate phases of inquiry—a practice that is consonant with the PADI project’s emphasis on creating blueprints for measuring scientific inquiry. One disadvantage, however, was that NSES inquiry standards do not explicitly reflect content knowledge (National Research Council, 1996). Our team grappled somewhat with the possible SMVs of a Student Model based on the NSES inquiry standards. Would each of the eight inquiry standards be considered an SMV? Would the standards be combined in some logical way to create a smaller number of SMVs? Would we create SMVs on the basis of the substandards (potentially 24 variables)? The larger the number of variables to be calibrated, the less precision of measurement was likely. Therefore, we could not be certain that Student Models with large numbers of SMVs would be workable.

Ultimately, our team was attracted to the notion of considering Student Models for Floating Pencil based on the NAEP content-by-process framework (Allen, Carlson, & Zelenak, 1999). This approach had a number of advantages. The NAEP framework guided the development of NAEP items and item groups and is widely understood in the assessment community. The content and process codes were available for the Floating Pencil items/item groups as well as for the other NAEP items involved in the calibration plans (Allen, Carlson, & Zelenak, 1999). This approach, however, had some disadvantages. The breadth of categories within the NAEP framework was not expected to yield measures that reflect the nature of students’ cognitive

14 The Floating Pencil task will be calibrated with other items from the Validities of Standards-Based Science Inquiry Assessments: Implementation Study.
15 Table 1 indicates the alignment between Floating Pencil items/item groupings and the NSES inquiry standards.
processes on the Floating Pencil task; also, NAEP’s process categories (conceptual understanding, practical reasoning, and scientific investigation) were not likely to yield measures that differentiated scientific inquiry processes.

4.2.2 Choice of Student Model

For the Floating Pencil task specification, our team chose to base the Student Model on the NAEP framework. The content and process codes from NAEP’s framework became the underlying variables of our Student Model. As we developed our Student Model, we considered a number of issues. We had some discussion as to whether conceptual understanding was distinct from types of content knowledge and considered dropping conceptual understanding as a process dimension. Because every NAEP item is coded for one of three content areas, it did not seem that the conceptual understanding dimension could be modeled as orthogonal to the content dimensions. We dropped the content area life sciences from our Student Model because none of the Floating Pencil items and none of the larger group of items Floating Pencil was to be calibrated with were life sciences items. It was noted that dropping this content area left us with only a subset of the NAEP framework. Finally, we defined six SMVs based on every possible content/process combination within the subset:

- Conceptual understanding within earth and space sciences
- Conceptual understanding within physical sciences
- Practical reasoning within earth and space sciences
- Practical reasoning within physical sciences
- Scientific investigation within earth and space sciences
- Scientific investigation within physical sciences

The rationale for defining SMVs in this manner will be discussed in a subsequent section of the report that considers the Measurement Model.

Our team coded information about the Student Model and SMVs into three areas of the task specification. The first two are found on the summary page (Appendix B): (1) under Student Model Summary we noted our use of the NAEP framework and its associated content and process codes, and (2) under Student Models we created a link to the actual Student Model named NAEP Floating Pencil Content and Process. The third area is found within the Student Model, where we defined and linked to the six SMVs listed above (see Figure 3). Figure 4 provides an example of one of the SMVs, conceptual understanding within earth and space sciences. This SMV is summarized in terms of content (e.g., solid earth, air, water) and in terms of conceptual understandings (e.g., knowledge of principles, laws, and theories). Objects in Figure 4 also include minimum and maximum of ability estimates on the standard Item Response Theory (IRT) scale (defined with a mean of 0 and standard deviation of 1). Although ability estimates may theoretically range from negative to positive infinity, the range of the ability estimates is typically restricted to the interval [-3.00, +3.00].
Figure 3. Student Model for Floating Pencil Task Specification

There are six SMVs that pertain to the content and process areas of the NAEP framework. Three dimensions involve physical science: conceptual understanding within physical science, practical reasoning within physical science, and scientific investigation within physical science. Three dimensions involve earth & space science: conceptual understanding within earth & space science, practical reasoning within earth & space science, and scientific investigation within earth & space science.

Figure 4. Student Model Variable for Floating Pencil Task Specification

NAEP Conceptual Understanding within Earth and Space Sciences: This SMV focuses on objects and events that are relatively accessible or visible. The concepts and topics covered are: solid earth, water, air, and the earth in space.

NAEP Practical Reasoning within Earth and Space Sciences: This SMV focuses on basic knowledge and understanding concerning the structure of the universe as well as the physical principles that operate within it.

NAEP Scientific Investigation within Earth and Space Sciences: This SMV focuses on objects and events that are relatively accessible or visible. The concepts and topics covered are: solid earth, water, air, and the earth in space.

NAEP Conceptual Understanding within Earth and Space Sciences: This SMV focuses on objects and events that are relatively accessible or visible. The concepts and topics covered are: solid earth, water, air, and the earth in space.

NAEP Practical Reasoning within Earth and Space Sciences: This SMV focuses on basic knowledge and understanding concerning the structure of the universe as well as the physical principles that operate within it.

NAEP Scientific Investigation within Earth and Space Sciences: This SMV focuses on objects and events that are relatively accessible or visible. The concepts and topics covered are: solid earth, water, air, and the earth in space.

There are kinds of me

I am a kind of

Done
To summarize, in creating a task specification for Floating Pencil, our team analyzed the task demands of the assessment and considered five potential Student Models. We chose a Student Model with SMVs based on the NAEP content-by-process framework and defined six SMVs based on process within content pairings. This choice has a number of advantages, such as being based on a broadly accepted framework, and disadvantages, such as lack of differentiation among science inquiry processes. Without results based on empirical data, however, it must be considered a working hypothesis. Will this Student Model exhibit sufficient model-data fit, or will modifications be required? Is this Student Model appropriate for a family of science performance assessment tasks such as the family outlined in Section 4.1.5 of this report?

### 4.3 The Evidence Model

The Evidence Model addresses the question of what student behavior(s) or performance(s) is expected to reveal what constructs of the Student Model. The Evidence Model lays out the argument for why and how the observations from a given task constitute evidence of scores or values on SMVs. The Evidence Model includes the evaluative submodel and the statistical submodel. The evaluative submodel provides the rules for evaluating evidence; this evaluative process results in Observable Variables. The statistical submodel describes a mathematical function that relates an Observable Variable to one or more SMVs. Note that what is known as the statistical submodel in the ECD framework is referred to as the Measurement Model in the PADI design system; both of these terms refer to psychometric models. In defining the Evidence Model for Floating Pencil, our team considered the Evaluation Procedures, Evaluation Phases, Observable Variables, and Measurement Model, as well as the relationship of the Evidence Model to the Student Model and the Task Model. These assessment objects are shown in Figure 1.

#### 4.3.1 The Evaluative Submodel

The evaluative submodel for Floating Pencil was chosen to mirror the NAEP rubric for Floating Pencil. Based on the NAEP rubric, the 14 Floating Pencil items were grouped into 10 scorable Work Products. The Floating Pencil team used these items and item groupings as the basis for defining 10 Activities within the Floating Pencil task (see the section on Task Models). For Floating Pencil, Table 3 provides the evaluative schemes, score levels, and Observable Variables (OVs) for each Activity. Work Products (part of the Task Model) serve as input to the Evaluation Procedures. These procedures, the evaluative schemes in Table 3, are used to convert Work Products into Observable Variables. Using the example of Activity 1, the Work Products, which are open-ended responses, are evaluated in a single Evaluation Phase and given scores of 4 = Complete, 3 = Essential, 2 = Partial, or 1 = Unsatisfactory/Incomplete (see Figure 5). These scores are the Observable Variables. Each of the 10 Work Products is directly converted into an Observable Variable in a single Evaluative Phase (evaluation submodels for other task specifications could include multiple Evaluative Phases in which output Observable Variables from one phase serve as Input Observable Variables for a subsequent phase). Therefore, each Floating Pencil Activity is associated with only one unique Evaluation Phase.
Figure 5. Evaluation Phase for Floating Pencil Activity 1

Our team coded information about the evaluation submodel into three areas of the Floating Pencil *task specification*: (1) under Evaluation Procedures Summary on the summary page (Appendix B), we noted our choice to use the NAEP rubric for evaluation; (2) within each Activity under Evaluation Procedures, we summarized the evaluative procedures for each Activity and created links to one Evaluation Phase object for each Activity; (3) within each Evaluation Phase object, we summarized the evaluation phase, linked to the appropriate Work Products and Output Observable Variables, and defined the Evaluation Action Data—the mapping between qualities of Work Products and Output Observable Variables (for example, see Figure 5). In doing this, we created and added to the PADI design system 10 new Observable Variables, one for each Evaluation Phase within each Activity.

### 4.3.2 Statistical Submodel

The Measurement Model, or statistical submodel, is a mathematical description of the relationship between Observable Variables (evidence of student proficiencies) and Student Model Variables (underlying constructs to be measured). In working with the PADI design system, Measurement Models are defined within Activities; each Activity has a unique Measurement Model (see Figure 1) that specifies Observable Variables, Student Model Variables, and the mathematical relationship between them.

For each Activity within Floating Pencil, Observable Variables are defined as the score levels resulting from evaluation of the Work Products. From Table 3, it can be seen that the Observable Variables can assume a range of values representing levels of response quality: for Activities 1, 2, and 10, the values 1, 2, 3, and 4; for Activities 3, 4, 6, and 8, the values 1, 2, and 3; and for Activities 5, 7, and 9, the values 0 and 1. As an example, Figure 6 presents the Observable Variable object linked to Activity 1. It should be noted that Activities or items with
two possible response levels are dichotomous, and those with three or more response levels are polytomous.

Figure 6. Observable Variable for Floating Pencil Activity 1

Our team gave considerable thought to the definition of the Student Model for Floating Pencil, and our initial definition can be considered a testable hypothesis. The NAEP framework provides three content and three process codes for this group of items (e.g., see Table 5). We chose to use these codes as the starting point for our Student Model and defined a six-dimensional Student Model (see Section 4.2.2). This model has six SMVs based on every possible content/process combination (excluding life sciences) found in the Floating Pencil Activities and the other items slated for calibration with Floating Pencil. Defining each content/process combination as a single SMV reflects the nature of inquiry-based science practices—that scientific inquiry occurs within particular domains of content and requires knowledge integration (e.g., Linn, Songer, & Bat-Sheva, 1996; National Research Council, 1996). Since each Activity is linked to only one SMV, the associated Measurement Models are defined as unidimensional. However, a psychometric model for the whole of Floating Pencil (plus the additional items to be calibrated) would exhibit between-item multidimensionality because the collection of Floating Pencil Activities (and additional items to be calibrated) has multiple measures of each SMV. For example, Activities 1, 6, and 9 measure conceptual understanding within earth and space sciences. This definition of Student Model deviates from NAEP’s scoring practices in 1996, in which scores for most items were based on only the content areas, ignoring the process distinction (Allen, Carlson, & Zelenak, 1999).

We considered various characteristics of the psychometric model. We assumed that the mathematical function linking underlying ability level (SMV) to the probability of a particular response level would be a logistical function. The BEAR Scoring Engine, which is currently the...
only scoring engine linked to the PADI design system, assumes the Multidimensional Random Coefficients Multinomial Logit (MRCML) model—a multidimensional Rasch model (Kennedy, 2005). This model can handle both dichotomous and polytomous scoring, as well as conditional dependencies among the items. We considered the advantages and disadvantages of other psychometric models for our data, including a multidimensional three-parameter logistic (3PL) model that would estimate slope and guessing parameters for the items. Although use of a multidimensional 3PL model was attractive, a scoring engine based on that model is not yet available, and the BEAR Scoring Engine has been used effectively by other PADI strands. The choice of a multidimensional Rasch model was a deviation from NAEP’s use of a 3PL scoring model in 1996 with Floating Pencil (Allen, Carlson, & Zelenak, 1999).

Our team coded information about the statistical submodel into three areas of the Floating Pencil task specification: (1) under Measurement Model Summary on the summary page (Appendix B), we noted our choice to use a unidimensional Rasch model to describe the probability of an observed score as a function of ability level on the SMV; (2) within each Activity under Measurement Models, we noted that a Rasch model relates the observed score on each Activity to the corresponding SMV; (3) within each Measurement Model object (for example, see Figure 7), we summarized the model, specified the model type (e.g., partial credit, dichotomous), linked to the Observable Variable and Student Model Variable, and specified a Scoring Matrix, a Design Matrix, and Calibration Parameters. The Scoring Matrix provides information about the weighting of a score with regard to each of the SMVs, the Design Matrix reflects the difficulty in moving from one score value to another, and the Calibration Parameters (typically thought of as item difficulties) are required to estimate student proficiencies (values of SMVs) from students’ scores for responses to items (values of OVs). In defining a Measurement Model for each of the 10 Activities, we created and added 10 new objects to the PADI design system.

**Figure 7. Measurement Model for Floating Pencil Activity 1**
The Measurement Model specified for each item requires that the item scores are conditionally independent. But this assumption is not likely to be met with the Floating Pencil task since all items are based on a common set of stimuli (i.e., task directive and physical materials) and some of the items are sequentially dependent—that is, the Work Product from one Activity serves as stimulus material for a subsequent item. One way to handle a subset of items that do not meet the assumption of conditional independence is to “bundle” the items into a single score, independent from other scores in the larger set. We discussed how to handle “bundling” Floating Pencil Activities, noting that such “bundling” may produce some “within-bundle” multidimensionality, depending on the SMVs of the Activities within each bundle. We were unable to determine conclusively whether NAEP treated the Floating Pencil Activities as statistically dependent or independent, although we believe that NAEP could not assume statistical independence, since Floating Pencil items were not included in NAEP IRT scaling procedures in 1996.

To summarize, the Evidence Model specifies how evidence is to be evaluated and the psychometric relationship between observed evidence and underlying theoretical constructs. Our team chose the evaluative submodel for Floating Pencil to mirror the NAEP rubric for Floating Pencil; on this basis, we grouped the 14 Floating Pencil items into 10 scorable Work Products. We defined a unidimensional Rasch Measurement Model for each Activity. We noted that a psychometric model for the whole of Floating Pencil would exhibit between-item multidimensionality; we also discussed the lack of conditional independence among items and considered “bundling” Floating Pencil activities. This choice of a psychometric model raises a number of issues, such as the strength of the relationship between OVs and SMVs and the adequacy of the Measurement Models. In addition, subsequent consideration should be given to the adequacy of the Evidence Model for a family of science performance assessment tasks (of which Floating Pencil is a member).
5.0 Summary and Discussion

Our reverse engineering and analysis of the Floating Pencil task was largely an epistemological process that involved grappling with task complexity in the context of PADI. Our team came to understand the characteristics and underlying assessment argument of the Floating Pencil task, the ECD framework within the context of the PADI design system, and the properties of the PADI design system. Through this process, we also came to new understandings of the design process for large-scale performance assessment tasks. The developmental needs of the project and the coupling of work—including the use of team members’ expertise and the balancing of team and individual learning curves—were managed by the team leaders. The Web-based PADI design system served as a repository of emerging knowledge, and changes to our task specification were immediately available to all team members. Our work left a trace in the form of the NAEP Floating Pencil task specification, contained in the PADI library. The Floating Pencil team’s work also affected the PADI design system. For example, a number of new Work Products and Student Model Variables were added to the system to accommodate the Floating Pencil task. Our team’s work also prompted discussions about the adequacy of the PADI design system as a development tool (e.g., making additional scoring engines available, eliminating redundancies within the PADI library).

The purpose of reverse engineering is to create a design or blueprint by analyzing a final product or system. In the case of reverse engineering an assessment by using the PADI design system, the final product is the assessment task itself, and the design or blueprint is an object in the form of a task specification, template, or design pattern. Specifying the design or blueprint involves explicating the understanding of an underlying assessment argument. In some cases, the task developer may have previously articulated a clear assessment argument. In other cases, such as with Floating Pencil, the reverse engineering process includes construction of this argument.

5.1 Proposed Assessment Argument for Floating Pencil

What is the assessment argument for Floating Pencil? There is no evidence that NAEP explicitly constructed an assessment argument for Floating Pencil, prior to its administration in 1996. Throughout the reverse engineering process, we have sought to adhere to NAEP’s purposes and decisions; therefore, we will consider an assessment argument based on NAEP’s goals for administering a large-scale reference examination. The Floating Pencil task was one among many tasks and items administered as part of the NAEP. The NAEP tasks and items were tied to the NAEP content-by-process framework (Allen, Carlson, & Zelenak, 1999). Student responses to tasks and items were considered evidence of the scientific content and process skills given in the framework. Therefore, an assessment argument for Floating Pencil might look something like the one provided in Figure 8.
Figure 8. Assessment Argument for Floating Pencil

<table>
<thead>
<tr>
<th>Evidence Model</th>
<th>Students’ responses to Floating Pencil items (Activities), such as multiple-choice items, open-ended items, and numerical response items, provide evidence for</th>
</tr>
</thead>
<tbody>
<tr>
<td>Student Model</td>
<td>students’ conceptual understandings within earth and space sciences and within physical sciences, students’ practical reasoning within earth and space sciences and within physical sciences, and students’ scientific investigation within earth and space sciences and within physical sciences.</td>
</tr>
<tr>
<td>Task Model</td>
<td>The warrant for this claim is that accepted understandings of the development of science ability posit that students can acquire the knowledge, skills, and abilities (KSAs) that are required to complete the Floating Pencil task and that these KSAs can be elicited through a hands-on investigation, into the salt concentrations of various liquids, in which the research question has been posed and investigative procedures have been specified.</td>
</tr>
</tbody>
</table>

If we were to base the assessment argument on NAEP’s reported scores from the 1996 assessment, the assessment argument would be limited to measuring only content knowledge (Allen, Carlson, & Zelenak, 1999).

The above assessment argument could be expanded to include all the items and tasks on the 1996 NAEP, as well as the whole of the content-by-process framework. In such a case, student responses on a large set of items and tasks would be aggregated to serve as evidence for content knowledge and process skills. For the purpose of serving as a national reference exam that is an unbiased indicator of national achievement not linked to any particular curriculum, this assessment argument is at a sufficient level of generality. However, for the purposes of describing the Floating Pencil task alone and measuring aspects of scientific inquiry (PADI’s stated reason for existence), this assessment argument might be considered insufficient.

5.2 Considerations for Proposed Assessment Argument

Any assessment argument is open to criticism through logical analysis. We will consider the relationship of elements of the assessment argument. The Student Model is the target of the assessment—what is important to measure. For a strong assessment argument, the relationship among the Student Model and the Task and Evidence Models is necessarily clear and logical. In other words, there is a high level of correspondence between what is to be measured (i.e., Student Model Variables) and the evidence to be gathered through the measures (i.e., OVs and TMVs). In addition, that assessment argument should align with the overall purposes of the assessment. The NAEP framework specifies process codes of scientific investigation, practical reasoning, and conceptual understanding. Considering PADI’s focus on
scientific inquiry, these process codes may be inadequate. For example, Floating Pencil Activities 2 through 5, 8, and 10 are all coded as scientific investigation within the NAEP framework, whereas these Activities are coded as five different aspects of scientific inquiry based on the NSES inquiry standards (National Research Council, 1996; see Table 1). A differentiation of scientific inquiry processes is consistent with PADI’s goal of understanding and measuring scientific inquiry. We have hypothesized that there is a relationship between the observable student proficiencies elicited by the task (e.g., students’ concepts of density, measurement skills, data analysis skills) and the underlying SMVs (conceptual understanding, practical reasoning, and scientific investigation within physical science and earth and space science). To fully evaluate this hypothesis, the strength and adequacy of this relationship must be empirically investigated, alternative relationships must be considered, and our chosen psychometric model must be examined. We have yet to consider the adequacy of this proposed assessment argument as a basis for forward engineering science performance assessments.

This analysis leads to a number of considerations:

- Are there changes that can be made to better differentiate among science inquiry processes without abandoning NAEP’s purposes?
- Are our proposed Student Models empirically supported? Is our Measurement Model adequately specified? If so, what can we learn?
- In what ways does our reverse engineering work shed light on forward engineering performance assessment tasks?

As we constructed our Student and Measurement Models, we used NAEP’s framework and reporting practices as a starting point—stepping forward in ways that might lead to a stronger assessment argument. On the basis of the NAEP framework, we calculate scores for Floating Pencil were based on only two content areas: earth and space sciences and physical sciences. Our proposed Student Model is composed of six SMVs—each a combination of content and process. Thus, our analyses may have sufficient power to distinguish among process variables (conceptual understanding, practical reasoning, and scientific investigation) as well as content variables. In addition, the embedding of process within content is in keeping with actual practices in the field of science education (National Research Council, 1996). However, the process variables do not distinguish among phases of scientific inquiry. A further developmental step might be defining sets of SMVs representing different scientific inquiry processes, perhaps on the basis of the NSES inquiry standards. A Student Model might be constructed and tested that contained a set of content variables (e.g., physical sciences and earth and space sciences) crossed with a set of inquiry variables (e.g., design and conduct a scientific investigation; use appropriate tools and techniques to gather, analyze, and interpret data; develop descriptions, explanations, predictions, and models using evidence; and think critically and logically to make the relationships between evidence and explanations).

Our current Student Model is a testable hypothesis. Data from this version of the Floating Pencil Assessment task and other large-scale science items were collected from 18 classes of middle school students. The Floating Pencil items are to be calibrated with a pool of large-scale science items made available in June 2005 through the SRI study of middle school science,
Validities of Standards-Based Science Inquiry Assessments: Implementation Study (see Quellmalz, et al., 2004; Quellmalz & Haydel, 2003; and Quellmalz & Kreikemeier, 2002). Our empirical work will involve testing the model fit of these data based on a number of Student Models (e.g., a two-dimensional model with content and inquiry variables). Empirical analyses will involve considering the model-data fit of various models and reinterpreting the SMVs. If a model is empirically supported, what can we learn? Here, we must consider the Task Model for Floating Pencil. We have made the argument that Floating Pencil is highly scaffolded. Therefore, even the most powerful and reliable measures of scientific investigation or inquiry will distinguish only a level of students’ abilities to correctly implement investigative procedures versus incorrectly implementing procedures, not their abilities to conduct an investigation in which the experimental procedures have not been specified. Similarly, the task requires limited content knowledge; therefore, measures of content knowledge are limited to small subsets of knowledge within physical science or within earth and space sciences. After having tested the Student Model empirically, we may be able to distinguish among students’ abilities to correctly implement prespecified investigative procedures and to distinguish among students’ levels of a limited domain of content knowledge. If the Student Model is not empirically supported, this could be due to a number of reasons that include: (1) the SMVs may not have a strong enough relationship to student proficiencies needed for the task; (2) there may be too many SMVs to be measured accurately; (3) the task may be too highly scaffolded for the student sample, such that there is little variation among student performances; (4) Task Model Variables not connected to the Student Model, such as the verbal demand of the task, may cause measurement error (in this case, these TMVs may serve as alternative hypotheses or counterclaims to the warrant for the assessment argument); or (5) the Measurement Model is misspecified.

Our reverse engineering work on Floating Pencil led us to consider the process of forward engineering additional performance assessment tasks. Toward that end, we have begun to draft an abstract template, a more generalized blueprint than a task specification, that could result in the design of multiple new performance assessments for eliciting inquiry skills and content knowledge. However, more development work is required to fine-tune the Evidence Model, Student Model, Task Model, and underlying assessment argument for this template. As this work comes to fruition, a task designer, with guidance from the PADI team, could use the template to make a number of decisions about potential tasks that would include specifying Task Model Variables (e.g., physical materials, verbal demand, level of content structure, level of inquiry structure, and cognitive complexity), Student Model Variables (within a generalized Student Model), the procedures for evaluating student Work Products, and options for the psychometric models relating Observable Variables to Student Model Variables.

The use of the PADI design system to reverse engineer the Floating Pencil task resulted in the creation of new knowledge about assessment, both general and specific, for our team. Since the principles of ECD are “hard-wired” into the PADI design system, we were supported in considering the coherence and linkages among the Task Model, Student Model, and Evidence Model (see Brecht, Mislevy, Haertel, & Haynie, 2005). Reverse engineering the Floating Pencil task not only contributed to our knowledge of the characteristics of one particular large-scale performance assessment task, but shed light on how new science performance assessments might be forward engineered. As our team conducts subsequent empirical analyses of Floating Pencil data; adjusts Task, Evidence, and Student Models; refines the underlying assessment
argument; and develops an abstract *template* for forward engineering science performance assessment tasks, we will continue to contribute to the developing knowledge base of task design through the principles of ECD.
References


APPENDIX A

Test Booklet for NAEP Floating Pencil
Middle School Science Test
“Floating Pencil”
Floating Pencil

For this task, you have been given a kit that contains materials that you will use to perform an investigation during the next 30 minutes. Please open your kit now and use the following diagram to check that all of the materials in the diagram are included in your kit. If any materials are missing, raise your hand and the administrator will provide you with the materials that you need.
Every body of water in natural ecosystems has salts and other substances dissolved in it. The concentration of dissolved salt varies from less than 0.2 percent in most freshwater streams and lakes to about 3.5 percent in most of the world’s oceans. In this task, you will observe and measure how much of the length of a pencil floats above the water surface in water with very low salt concentration and in water with very high salt concentration. You will then use the same procedures to estimate the salt concentration of an unknown solution. Follow the directions step-by-step and write your answers to the questions in the space provided in your booklet.
1. Open the plastic bottle labeled Water. The salt concentration of this water is very close to 0 percent. Pour the water into the cylinder up to the black line. Put the cap back on the bottle.

Now take the pencil and put it in the water in the cylinder, eraser-end down. Part of the pencil will float above the water, as shown in the picture below.

Explain why the pencil floats when it is put in the water.

__________________________________________________________________
__________________________________________________________________
__________________________________________________________________
__________________________________________________________________
__________________________________________________________________
__________________________________________________________________
__________________________________________________________________
2. Look at the pencil in the water. There are letters along the side of the pencil. Make sure that the pencil is not touching the side of the cylinder. Note the exact level where the water surface meets the side of the pencil, as shown in Picture A. Then draw a line on Picture B where the water surface comes to on your pencil. This line will help you to remember where the water level came to on your pencil for the next step (3).

![Picture A](image1.png)

![Picture B](image2.png)

3. Now take the pencil out of the water and dry it with a paper towel. Use the ruler to measure the length of the pencil that was above the water. Record the length in Table 1 below under Measurement 1.

<table>
<thead>
<tr>
<th>Type of Solution</th>
<th>Length of Pencil Above Water Surface (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Measurement 1</td>
</tr>
<tr>
<td>Water</td>
<td></td>
</tr>
<tr>
<td>Salt Solution</td>
<td></td>
</tr>
<tr>
<td>Unknown Solution</td>
<td></td>
</tr>
</tbody>
</table>
4. Now place the pencil back in the water and repeat steps 2 and 3. Record your measurement in Table 1 under **Measurement 2**.

5. Calculate the average of Measurements 1 and 2 and record the result in the data table.
   (You can calculate the average by adding Measurement 1 + Measurement 2 and then dividing by two.)

6. Explain why it is better to measure the length of the pencil that was above the water more than once.

   ____________________________________________________________
   ____________________________________________________________
   ____________________________________________________________
   ____________________________________________________________

Now pour the water out of the cylinder back into the bottle labeled “Water.” Put the cap back on the bottle.

Now open the plastic bottle labeled **Salt Solution**. This solution contains 25% salt. Pour the salt solution into the cylinder up to the black line. Put the cap back on the bottle.

7. Take the pencil and put it in the 25% salt solution in the cylinder, eraser-end down. How does the pencil float in this solution compared to how it floated in the water? (Circle the correct answer.)
   a. In the salt solution, more of the pencil is above the surface.
   b. In the salt solution, more of the pencil is below the surface.
8. Use the same procedure that you used with the pencil in the water to obtain two measurements of the length of the pencil that floats above the surface of the 25% salt solution. Record these two measurements in Table 1. Then calculate the average and record this result in the table.

9. Why does the pencil float at a different level in the salt solution than in the water?

________________________________________________________________
________________________________________________________________
________________________________________________________________
________________________________________________________________

10. If you added more salt to the 25% salt solution and stirred the solution until the salt was dissolved, how would this change the way that the pencil floats? (Circle the correct answer.)
    a. Less of the pencil would be above the surface.
    b. More of the pencil would be above the surface.
    c. There would be no difference in the amount of pencil above the surface.

Now pour the salt solution out of the cylinder back into the bottle labeled “Salt Solution.” Put the cap back on the bottle.

Now open the plastic bottle labeled Unknown Solution. You will now estimate the concentration of this unknown salt solution. Pour the unknown solution into the cylinder up to the black line. Put the cap back on the bottle.

11. Put the pencil in the solution in the cylinder, eraser-end down. Then repeat the same procedure that you used for the water and the salt solution. Obtain two measurements of the length of the pencil that floats above the surface of the unknown solution. Record these two measurements in Table 1. Then calculate the average and record this result in the table.
12. On the graph below, plot the average values you obtained for the water and the 25% salt solution. Draw a straight line between the two data points. Assume that this line represents the relationship between the length of pencil that is above the water surface and the concentration of salt in the water.
13. Based on the graph that you plotted, how does the length of the pencil that is above the surface change when the salt concentration changes? (Circle the correct answer.)
   a. It increases as the salt concentration increases.
   b. It decreases as the salt concentration increases.
   c. It remains constant as the salt concentration increases.

14. Based on the graph that you plotted, what is the salt concentration of the unknown solution?

________________

Explain how you determined your answer.

________________________________________________________________________________________
________________________________________________________________________________________
________________________________________________________________________________________
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________________________________________________________________________________________

Cleaning Up

- Wipe up any spilled liquids at your work area.
- Throw away all paper towels into the classroom trashcan.
- Pour all liquids from bottles into the bucket labeled “LIQUID WASTE ONLY”.
- Put all materials back into bag labeled “Floating Pencil Kit” and return it to the collection site identified by the test administrator.
Appendix B—Floating Pencil Task Specification Summary Page

NAEP Floating Pencil | Task Specification 1193

**Title:** NAEP Floating Pencil

**Summary:** This task specification is for the NAEP Floating Pencil Task. The task prompts students to conduct a hands-on investigation in which the research question has been posed and procedures have been specified. Students are asked to carry out experimental procedures following standard methods so that comparisons can be made, data summarized, predictions made, and explanations provided.

**Type:**

**Student Model Summary:** Based on the NAEP framework, there are six dimensions that pertain to the content and process areas of the framework. These dimensions involve physical science: conceptual understanding within physical science, practical reasoning within physical science, and scientific investigation within physical science. Three dimensions involve earth & space science: conceptual understanding within earth and space science, practical reasoning within earth and space science, and scientific investigation within earth and space science.

We did not include the content area of life sciences in this model, part of the NAEP framework, since Floating Pencil does not include items that measure life science content. We plan to consider other student models as well, including a model based on the NAEP standards, which are defined by analyses of the items, a two-dimensional model having a content and inquiry dimension, and a unidimensional model.

**Student Models:** NAEP Floating Pencil Content and Process. There are six SMs that pertain to the content and process areas of the NAEP framework. Three dimensions:

**Measurement Model Summary:** The unidimensional Rasch model describes the probability of an observed score as a function of ability level on an SMV.

**Evaluation Procedures Summary:** Evaluation will be carried out according to the NAEP procedures. This includes evaluating individual activities according to the NAEP rubric. In addition, other training and open-ended item scoring will be carried out according to standard NAEP procedures.

We will also consider different measurement models that will vary according to various student models and consider conditional dependencies between items. For bundled items, multi-dimensional models may be required.

**Work Product Summary:** Work products for Floating Pencil include:

- written explanations of concepts, observations, and procedures
- written responses to multiple-choice questions
- numerical measurements and averages in a data table
- plotted points and a drawn line on an X-Y graph
- a numerical estimate based on an X-Y graph of averages

**Task Model Variable Summary:** The following task-model variables are key:

- Physical Materials
- Level of scaffolding for inquiry
- Level of scaffolding for content
- Verbal demand
- Verbal sophistication
- Cognitive complexity
- Level of difficulty of inquiry
- Level of difficulty of content
- Level of extensiveness of inquiry
- Level of extensiveness of content

**Template-level Task Model Variables:**

- Physical Materials: This task model variable controls the physical materials for a given task—e.g., measurement tools.
- Level of scaffolding for inquiry: The level of scaffolding for carrying out a scientific investigation within a given task of activity.
- Level of scaffolding for content: The level of scaffolding for content within a given task or activity.
- Verbal demand: The level of verbal sophistication in the task stimulus and item prompts.
- Cognitive complexity: The overall cognitive complexity of the task, including the number of variables and data transformation.
- Level of difficulty of inquiry: The level of difficulty for conducting scientific inquiry or carrying out inquiry procedures.
- Level of extensiveness of inquiry: The extent of scientific inquiry within the task.
- Level of difficulty of content: The difficulty of the content within a given task or activity.
- Level of extensiveness of content: The extraextensiveness of content within a given task of activity.

**Task Model Variable Settings:**

**Materials and Presentation Requirements:** Laboratory equipment, solutions, and measuring instruments must be standardized across all students. Each student will receive a task booklet and a kit containing laboratory equipment. Each student will need adequate space to lay out the equipment, perform the measurements, and record results. Students will be required to read through and follow the instructions in the task booklet. Students will be required to write their answers in the task booklet. Students will be given 30 minutes to complete the task.

Continued
### Floating Pencil Task Specification Summary

**Appendix B—Floating Pencil Task Specification Summary Page**

<table>
<thead>
<tr>
<th>Materials and Presentation Settings</th>
<th>[ ]</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Activities Summary</strong></td>
<td>An activity is defined by a unique set of procedures that result in a single student score as defined by the 1996 NAEP Scoring Rubric. The Floating Pencil task has a total of 19 activities, covering a range of levels of cognitive demands for students.</td>
</tr>
<tr>
<td><strong>Activities</strong></td>
<td>Floating Pencil Activity 1: Student puts a pencil in a cylinder filled with water and explains why the pencil floats. Floating Pencil Activity 2: Student measures the length of the pencil above a liquid's surface. Floating Pencil Activity 3: Student calculates the average of two measurements. Floating Pencil Activity 4: Student explains that taking multiple measurements can reduce measurement uncertainty. Floating Pencil Activity 5: Student selects a response to a comparison question about how pencil floats in 2 different solutions. Floating Pencil Activity 6: Student explains why the pencil floats at a different level in a salt solution compared with water. Floating Pencil Activity 7: Student selects a response to a question about how the pencil's floating would change if more salt were added. Floating Pencil Activity 8: Student graphs their average values for water and 25% salt solution; student connects these 2 points. Floating Pencil Activity 9: Student selects a response to a question about how the length of the pencil above water changes when... Floating Pencil Activity 10: Student estimates the salt concentration of unknown solution; student describes how they determined...</td>
</tr>
<tr>
<td><strong>Tools for Examiner</strong></td>
<td>[ ]</td>
</tr>
<tr>
<td><strong>Exemplars</strong></td>
<td>E aide (Grade 8 Floating Pencil) PDF version of task can be found at:</td>
</tr>
<tr>
<td><strong>Educational Standards</strong></td>
<td>NAEP Bk 1: Design and conduct a scientific investigation. Students should develop general abilities, such as... NAEP Bk 2: Use appropriate tools and techniques to gather, analyze, and interpret data. The use of tools and... NAEP Bk 3: Develop descriptions, explanations, predictions, and models using evidence. Students should base the... NAEP Bk 4: Think critically and logically to make the relationships between evidence and explanations. Thinking... NAEP Bk 5: Use mathematics in all aspects of scientific inquiry. Mathematics is essential to asking and answering...</td>
</tr>
<tr>
<td><strong>Design Patterns</strong></td>
<td>Floating Pencil: This design pattern is for the NAEP Floating Pencil Task. The task prompts students to conduct a Yes... Conduct investigations: Students are presented with a scientific problem to solve or investigate and a solution strategy. Do... Design and conduct a scientific investigation: Students are presented with a scientific problem to solve or investigate. Do they effectively plan a...</td>
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<td><strong>I am a kind of</strong></td>
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<td><strong>These are kinds of me</strong></td>
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<td><strong>These are parts of me</strong></td>
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<tr>
<td><strong>Online resources</strong></td>
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<tr>
<td><strong>References</strong></td>
<td>NAEP 1996 Scoring Rubric</td>
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<tr>
<td><strong>I am a part of</strong></td>
<td>[ ]</td>
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</table>
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